

Illustrative Examples of Reactive Capability (D-Curves) and Corresponding Compensation under Package E

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Flat rate: a generator's revenue is $MVAR_Capability * Rate$

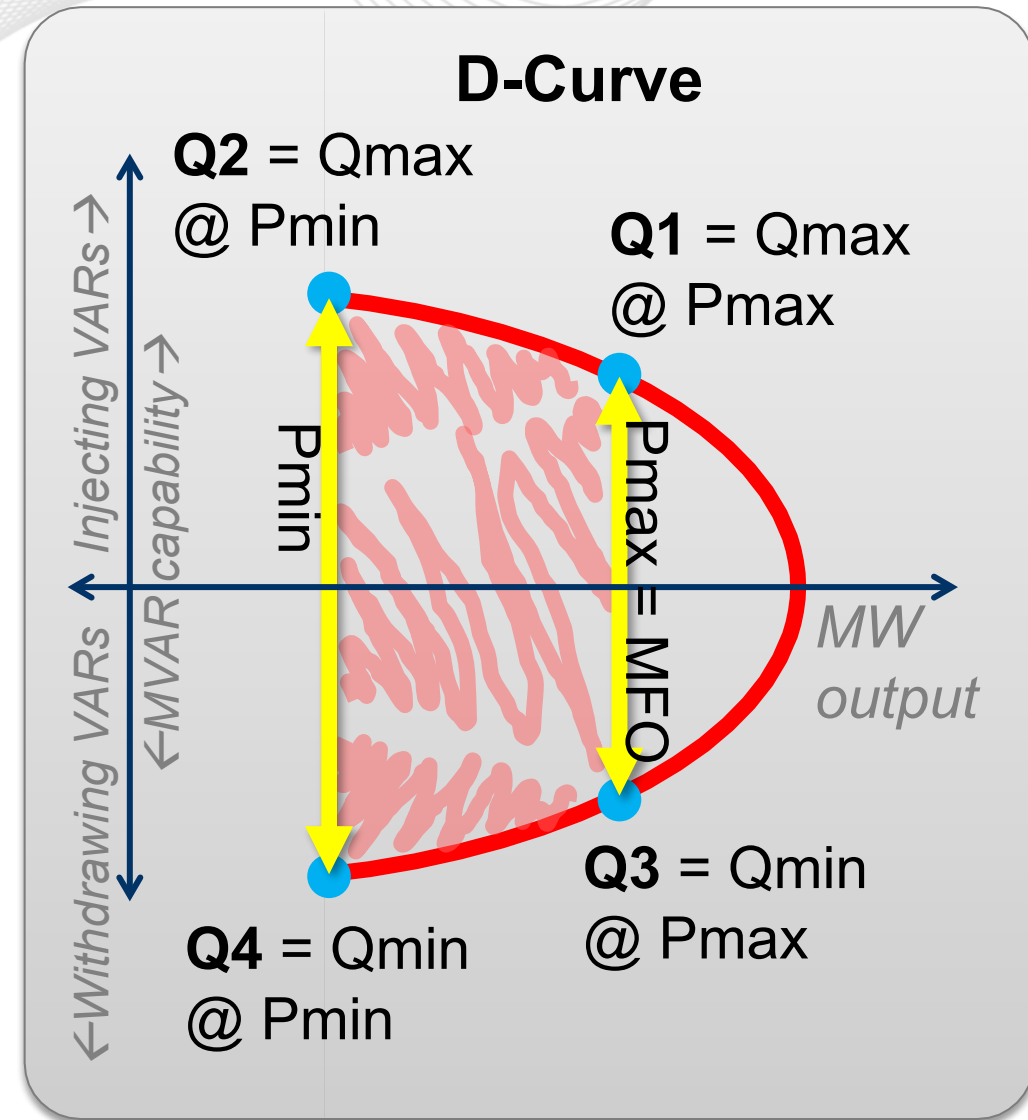
- For illustration, assume Rate is \$1,000/MVAR-yr (hypothetically).

A generator's **D-curve** shows the maximum reactive capability (both injecting & withdrawing VARs, or "Q") as a function of real power (i.e., MW or "P") output.

- In general, machine designs mean more MW output means less MVAR capability.

MVAR_Capability is [average of Q1 and Q2] minus [average of Q3 and Q4]. This basically amounts to: **injecting capability (averaged at Pmax and Pmin) plus withdrawing capability (averaged at Pmax and Pmin).**

- VAR withdrawal is negative Q, hence the "minus".
- Pmin is the lowest power the generator is capable of making while online (not less than zero).
- Pmax is Maximum Facility Output or the functional equivalent.

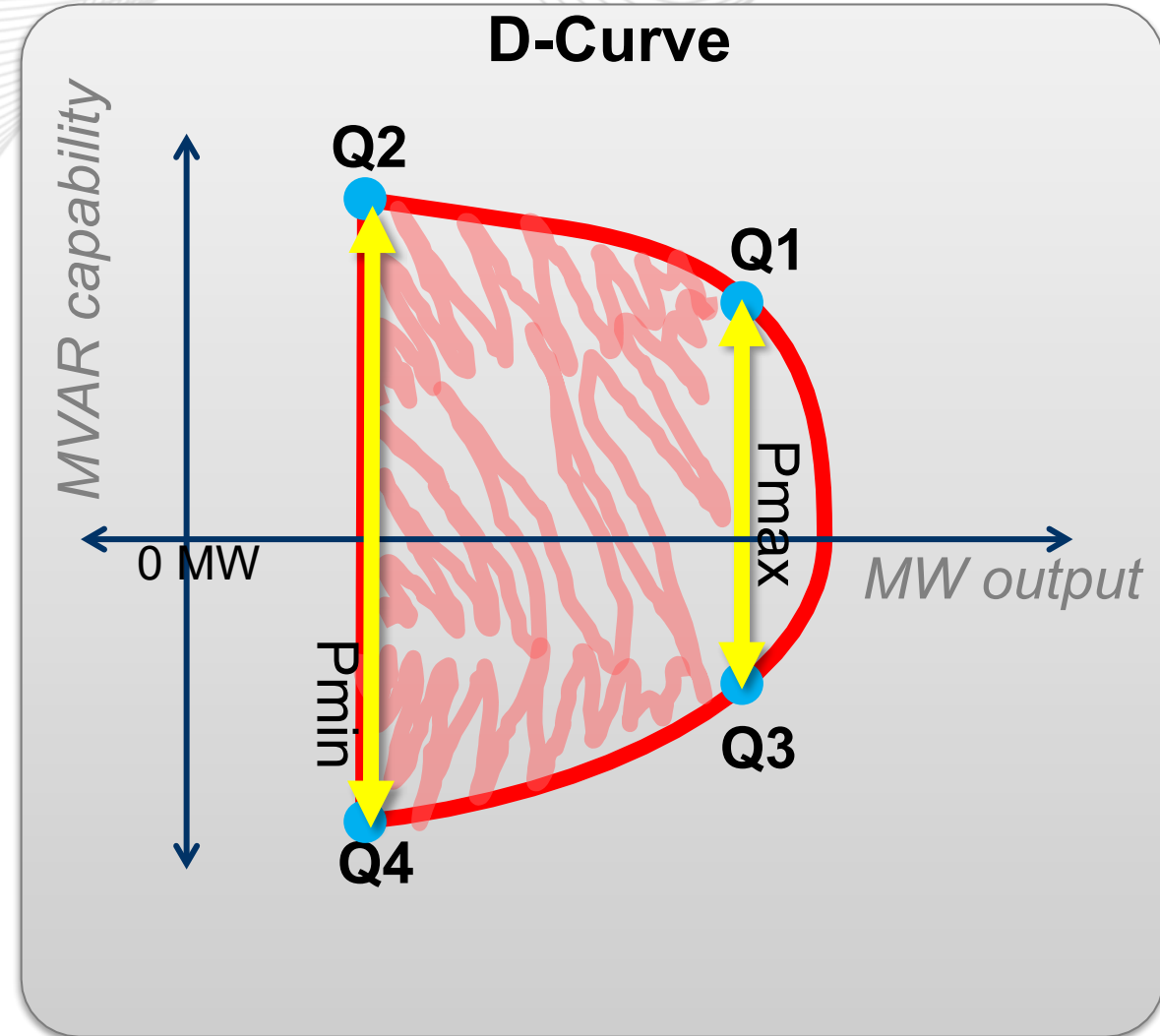


Illustrative Example of a 100 MW Steam Generator

- VAR injection capability:
 - Q1 at Pmax (100 MW) = **40 MVAR**
 - Q2 at Pmin (50 MW) = **50 MVAR**
- VAR withdrawal capability:
 - Q3 at Pmax = **-33 MVAR**
 - Q4 at Pmin = **-40 MVAR**
- Average(**40,50**) - Average(**-33,-40**) = 81.5
- Compensation = \$1,000*81.5 = **\$81,500/yr**

Typical interconnection agreements require a minimum reactive capability that amounts to roughly 1/3d of MFO. In theory, the “nose” of the D-curve is typically not available.

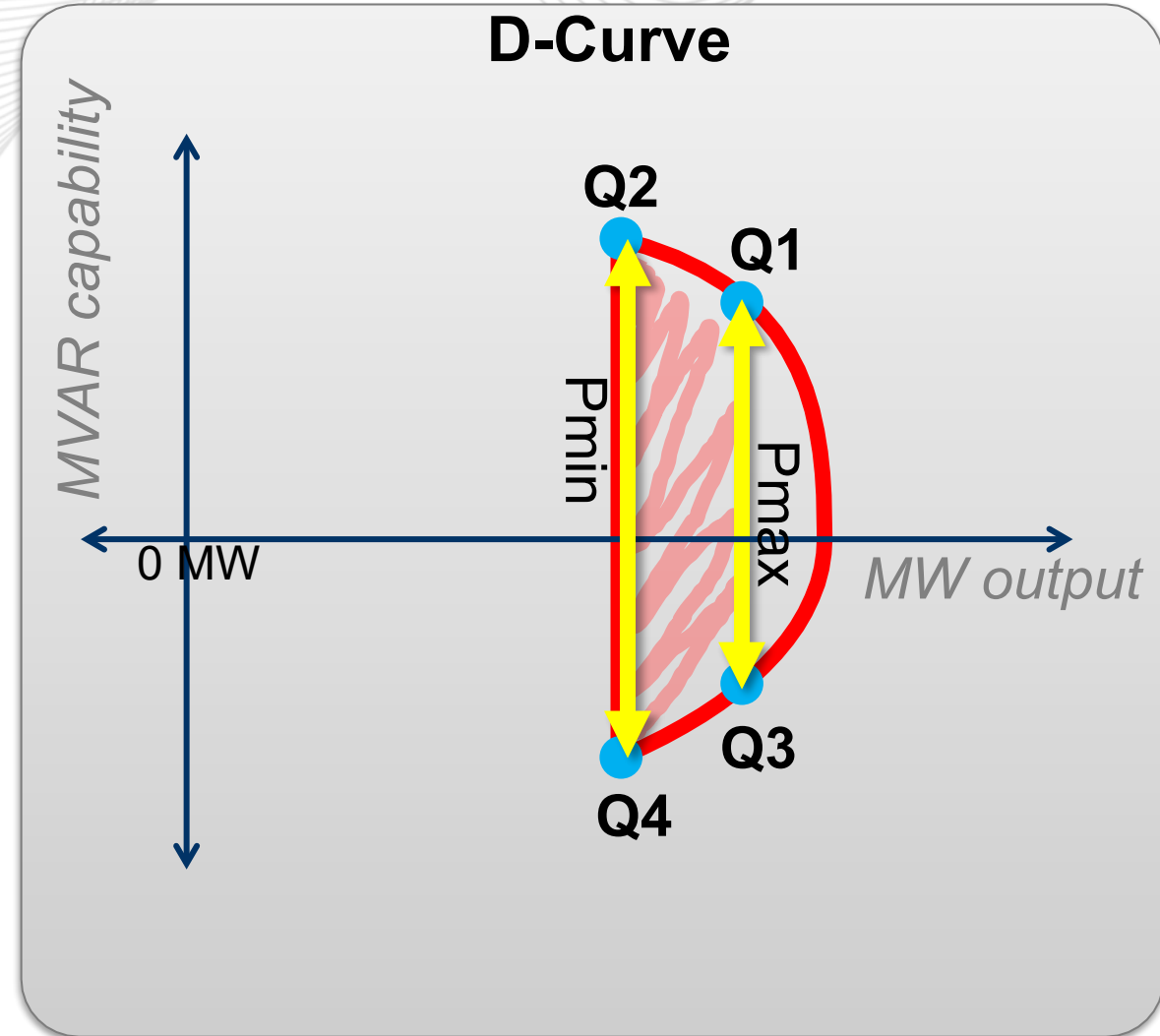
Synchronous machine designs generally have lower VAR withdrawal capability than injection capability.



Hypothetical rate of \$1,000/MVAR-yr

- VAR injection capability:
 - Q1 at Pmax (100 MW) = **40** MVAR
 - Q2 at Pmin (80 MW) = **45** MVAR
- VAR withdrawal capability:
 - Q3 at Pmax = **-33** MVAR
 - Q4 at Pmin = **-35** MVAR
- Average(**40,45**) – Average(**-33,-35**) = 76.5
- Compensation = \$1,000*76.5 = **\$76,500/yr**

A CT might have a narrower dispatchable range than a steam generator, which might reduce the reactive capability available to PJM.



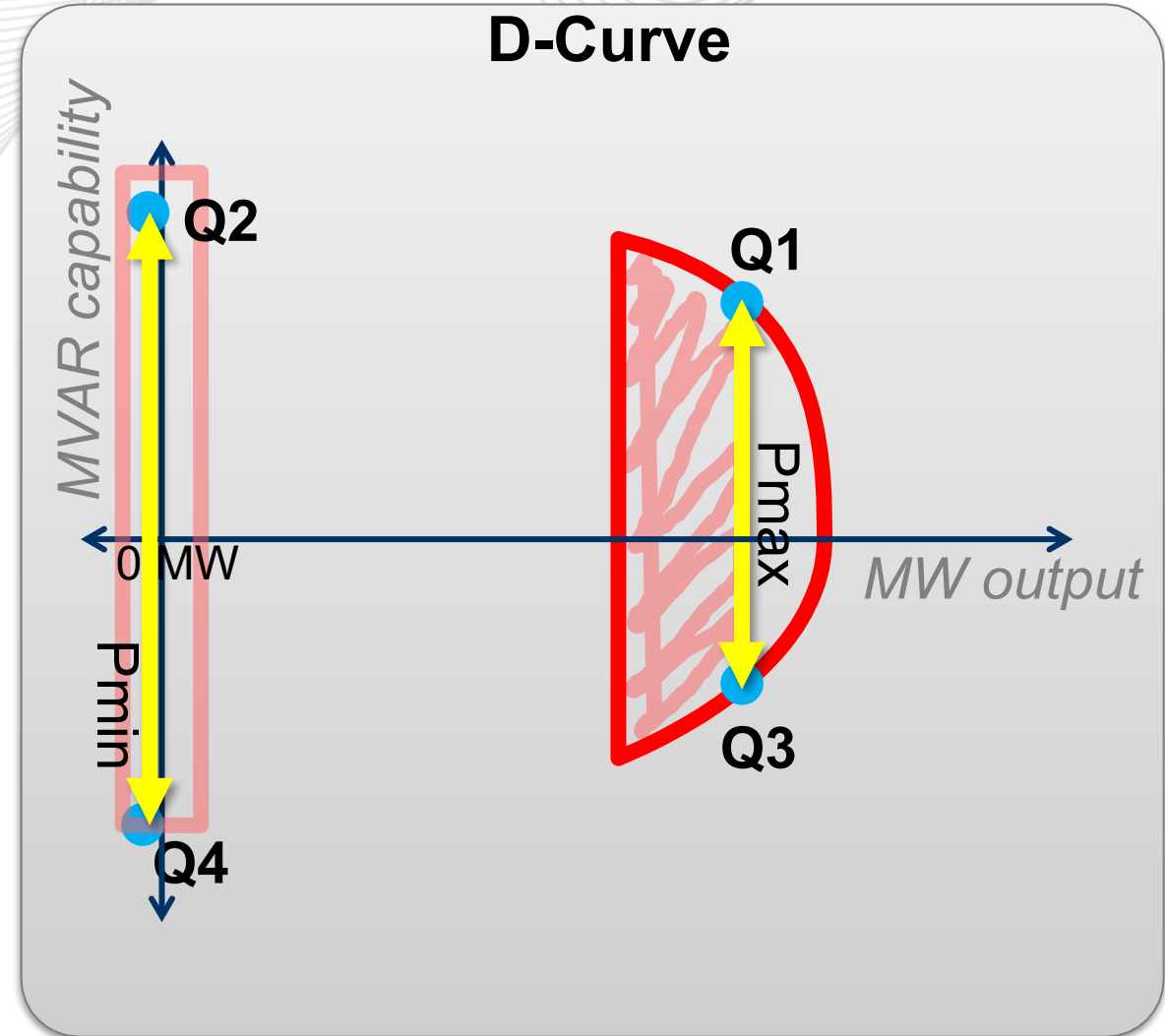
Hypothetical rate of \$1,000/MVAR-yr

Illustrative Example of a Combustion Turbine w/ Condensing Mode

A synchronous machine generator with “condensing mode” can operate at 0 MW.

- VAR injection capability:
 - Q1 = **40** MVAR
 - Q2 = **50** MVAR
- VAR withdrawal capability:
 - Q3 = **-33** MVAR
 - Q4 = **-40** MVAR
- Average(**40,50**) – Average(**-33,-40**) = 81.5
- Compensation = \$1,000*81.5 = **\$81,500/yr**

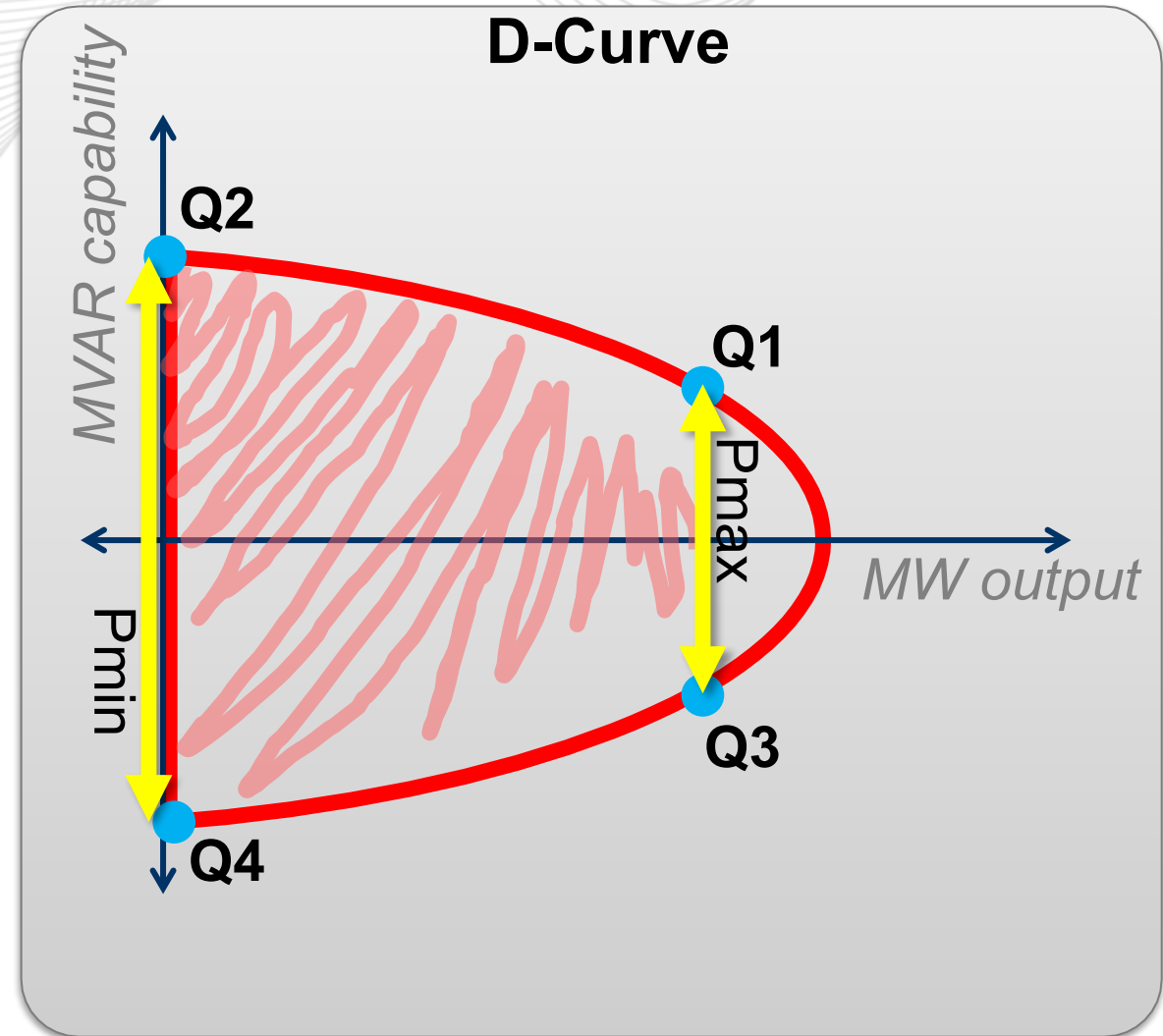
D-Curve



Hypothetical rate of \$1,000/MVAR-yr

- VAR injection capability:
 - Q1 = **33** MVAR
 - Q2 = **45** MVAR
- VAR withdrawal capability:
 - Q3 = **-33** MVAR
 - Q4 = **-45** MVAR
- Average(**33,45**) – Average (**-33,-45**) = 78
- Compensation = \$1,000*78 = **\$78,000/yr**

Inverter reactive capability matches power capability (they have a circular D-curve at the inverter terminals), however high impedance between PJM and large solar farm inverters reduces the reactive capability.



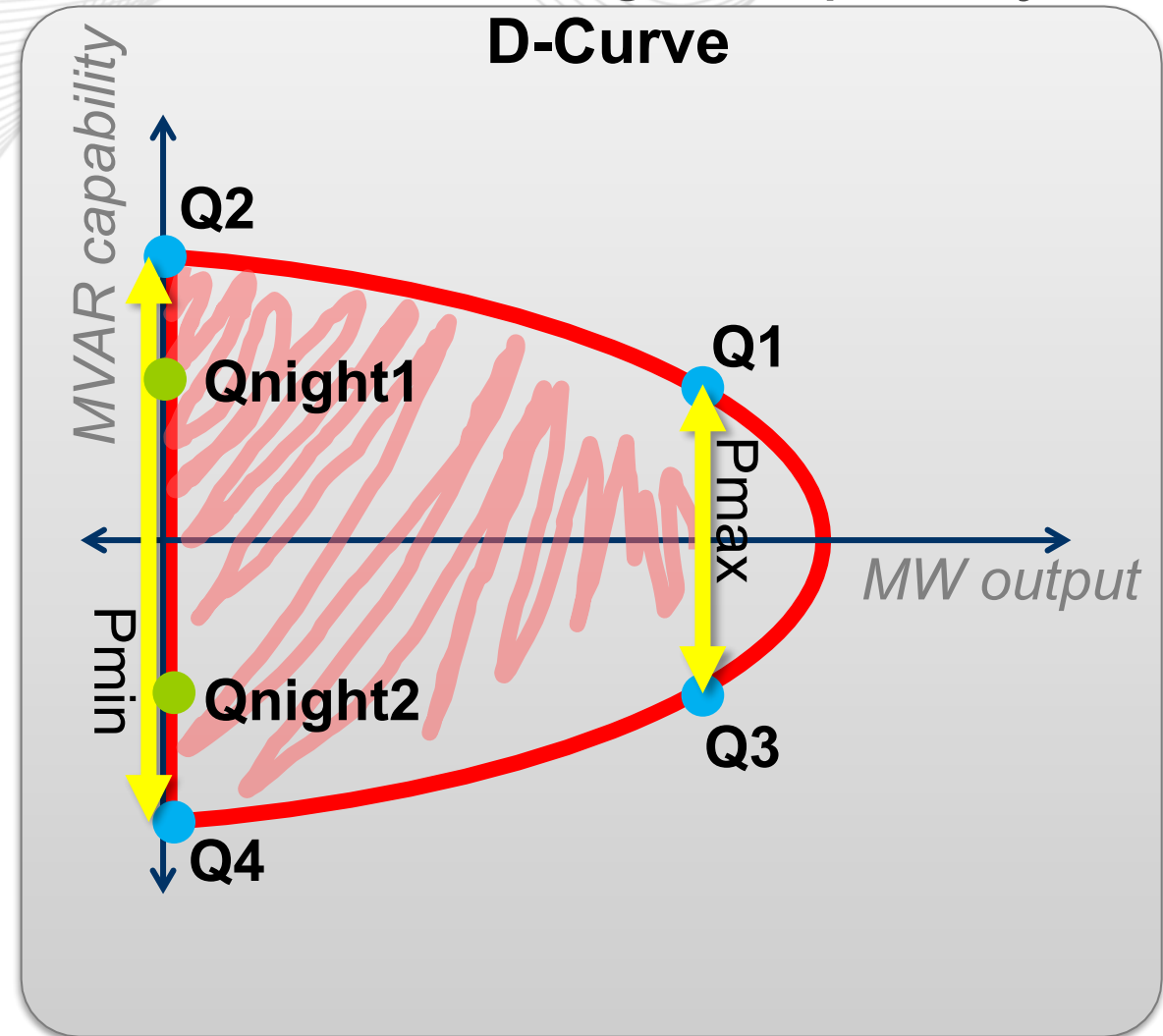
Hypothetical rate of \$1,000/MVAR-yr



Illustrative Example of a Solar Plant w/ Reactive at Night Capability

- VAR injection capability:
 - Q1 = **33** MVAR
 - Q2 = **45** MVAR
- VAR withdrawal capability:
 - Q3 = **-33** MVAR
 - Q4 = **-45** MVAR
- Average(**33,45**) – Average (**-33,-45**) = 78
- Compensation = \$1,000*78 = **\$78,000/yr**

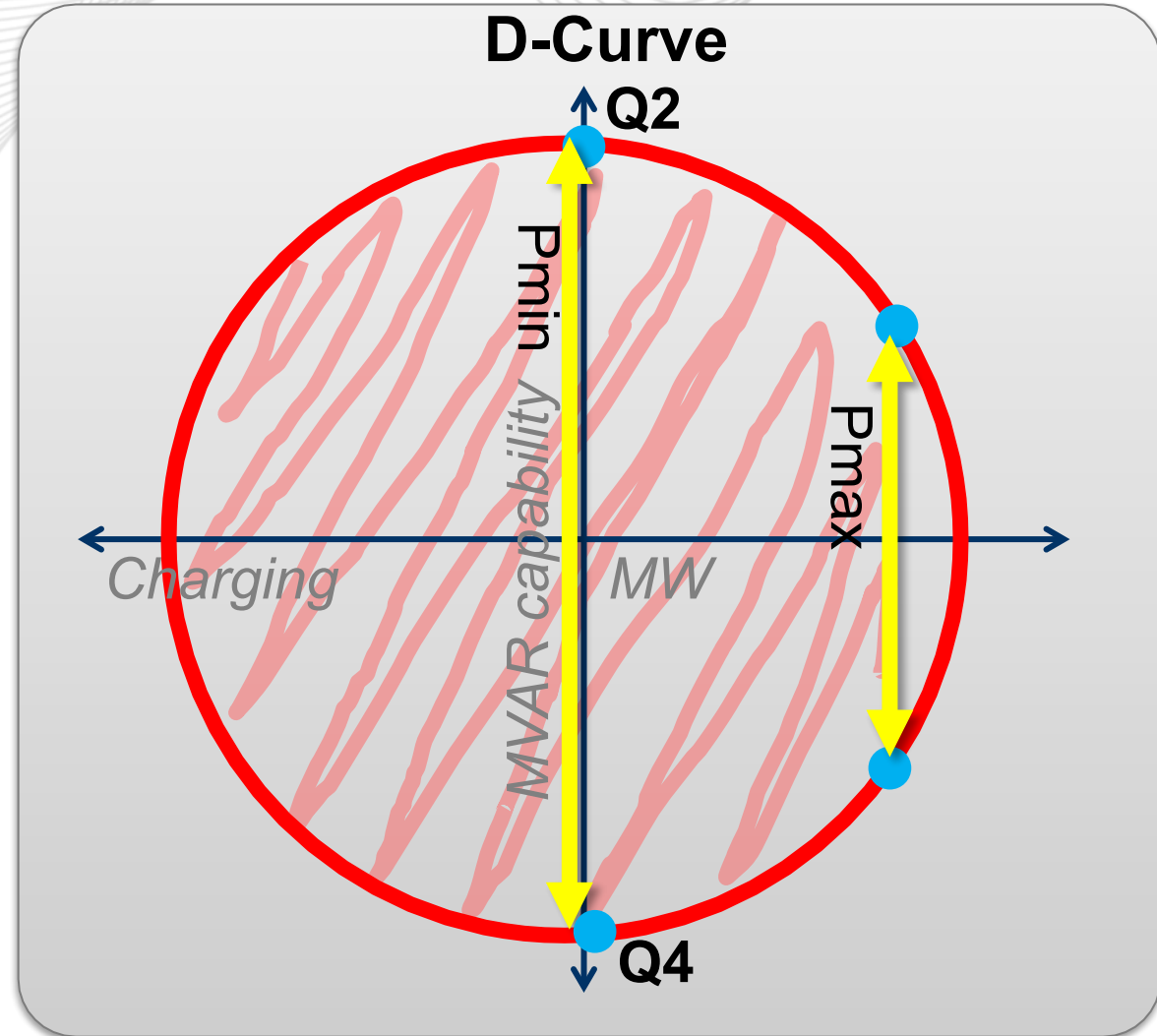
Reactive capability at 0 MW at night might be lower than capability at 0 MW during the day (i.e., when dispatched to 0 MW). Therefore, no change vs. previous example.



Hypothetical rate of \$1,000/MVAR-yr

- VAR injection capability:
 - Q1 = **33** MVAR
 - Q2 = **100** MVAR
- VAR withdrawal capability:
 - Q3 = **-33** MVAR
 - Q4 = **-100** MVAR
- Average(**33,100**) – Average (**-33,-100**) = 133
- Compensation = \$1,000*133 = **\$133,000/yr**

Battery inverters would be located close to the POI, with little impedance to PJM. The full circular inverter capability is therefore available to PJM.

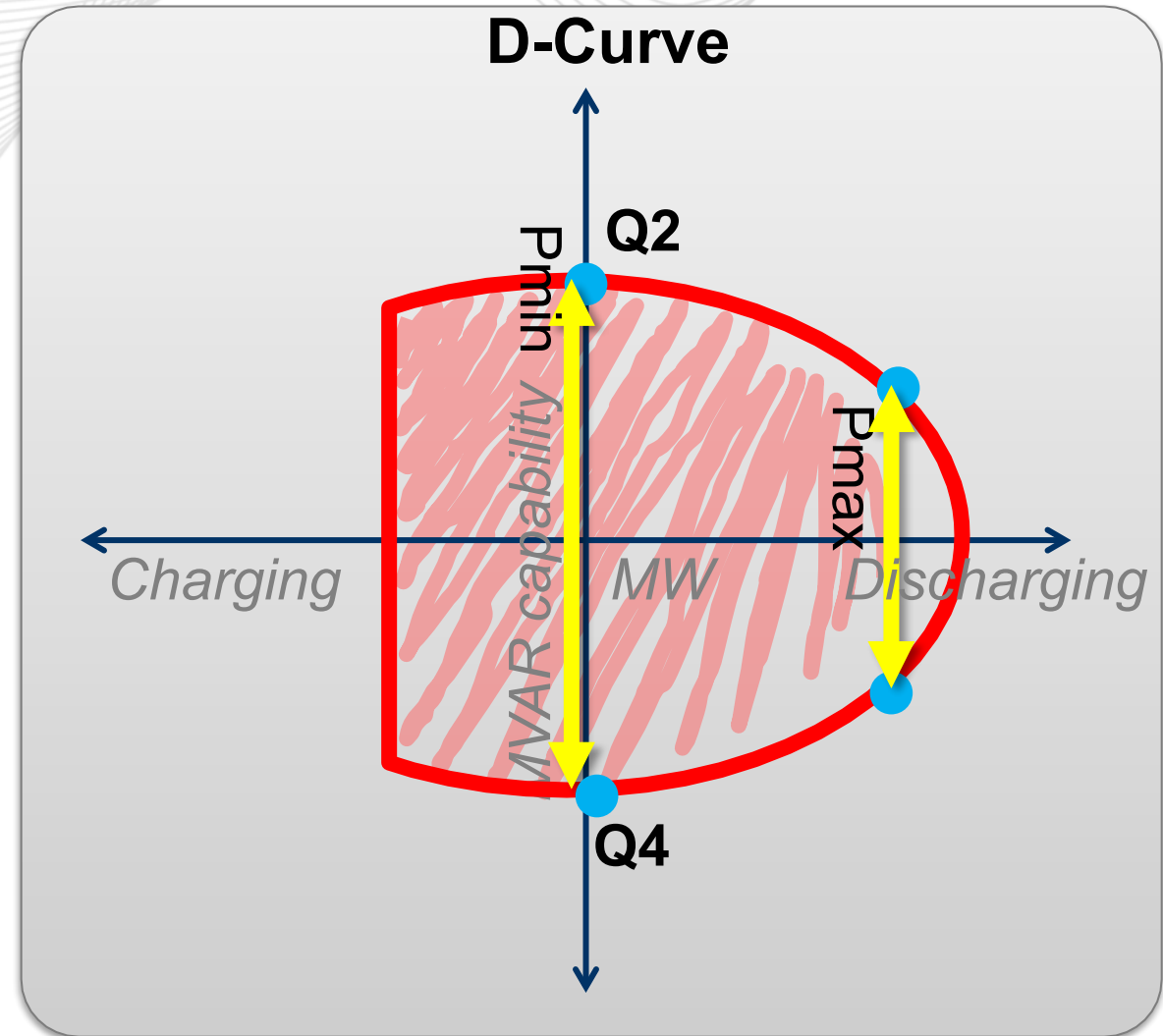


Hypothetical rate of \$1,000/MVAR-yr

Illustrative Example of a Solar-Battery Hybrid (Shared Inverters)

- VAR injection capability:
 - Q1 = **33** MVAR
 - Q2 = **45** MVAR
- VAR withdrawal capability:
 - Q3 = **-33** MVAR
 - Q4 = **-45** MVAR
- Average(**33,45**) – Average (**-33,-45**) = 78
- Compensation = \$1,000*78 = **\$78,000/yr**

This hypothetical solar-battery hybrid uses the solar inverters to operate the batteries. It is the same as the standalone solar example, except also has charging MW.

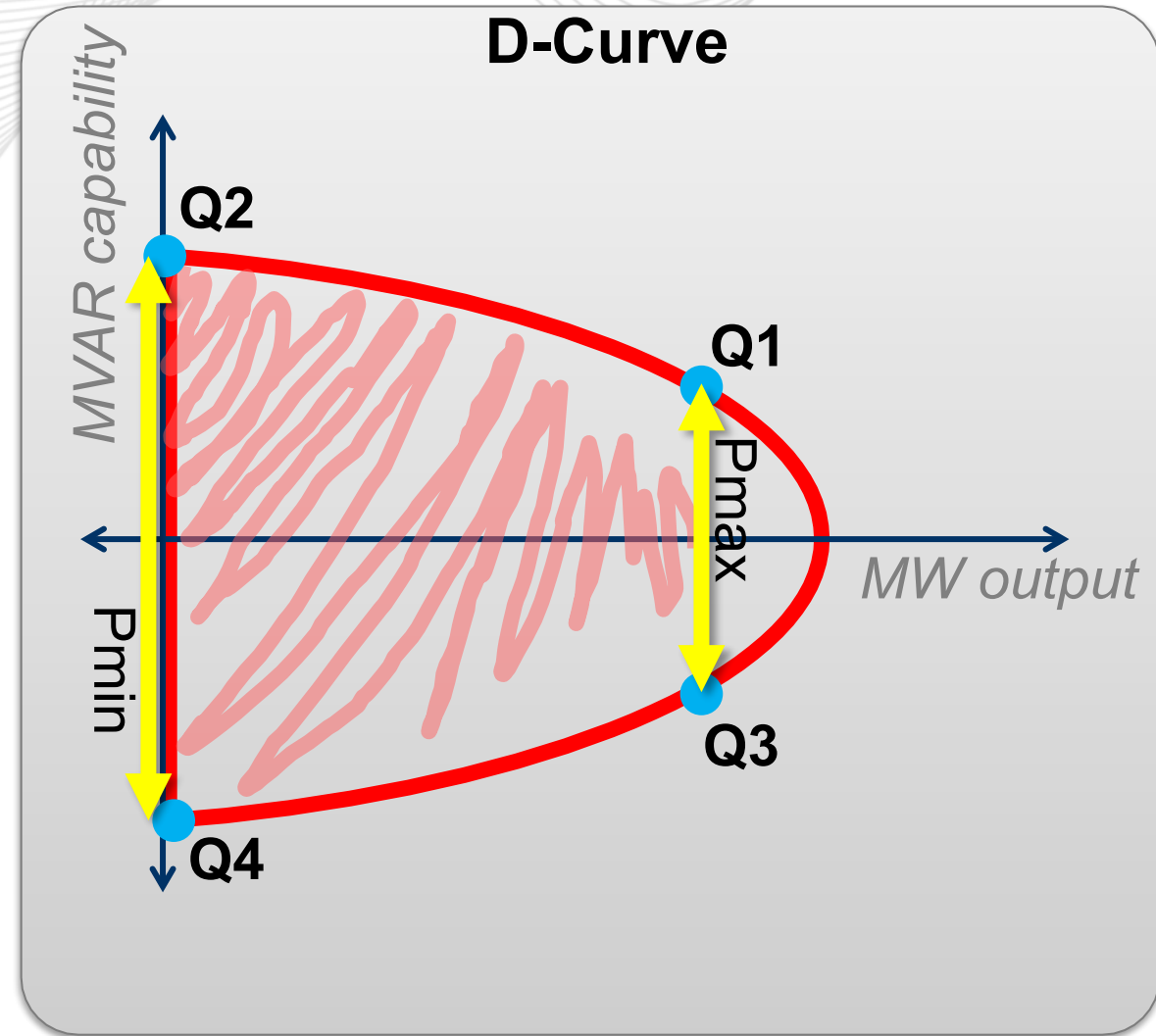


Hypothetical rate of \$1,000/MVAR-yr

Illustrative Example of New-Technology Wind Plant

- VAR injection capability:
 - Q1 = **33** MVAR
 - Q2 = **45** MVAR
- VAR withdrawal capability:
 - Q3 = **-33** MVAR
 - Q4 = **-45** MVAR
- Average(**33,45**) – Average (**-33,-45**) = 78
- Compensation = \$1,000*78 = **\$78,000/yr**

New wind generator technology is fully inverter-based, similar to solar. This result is the same as the solar example.

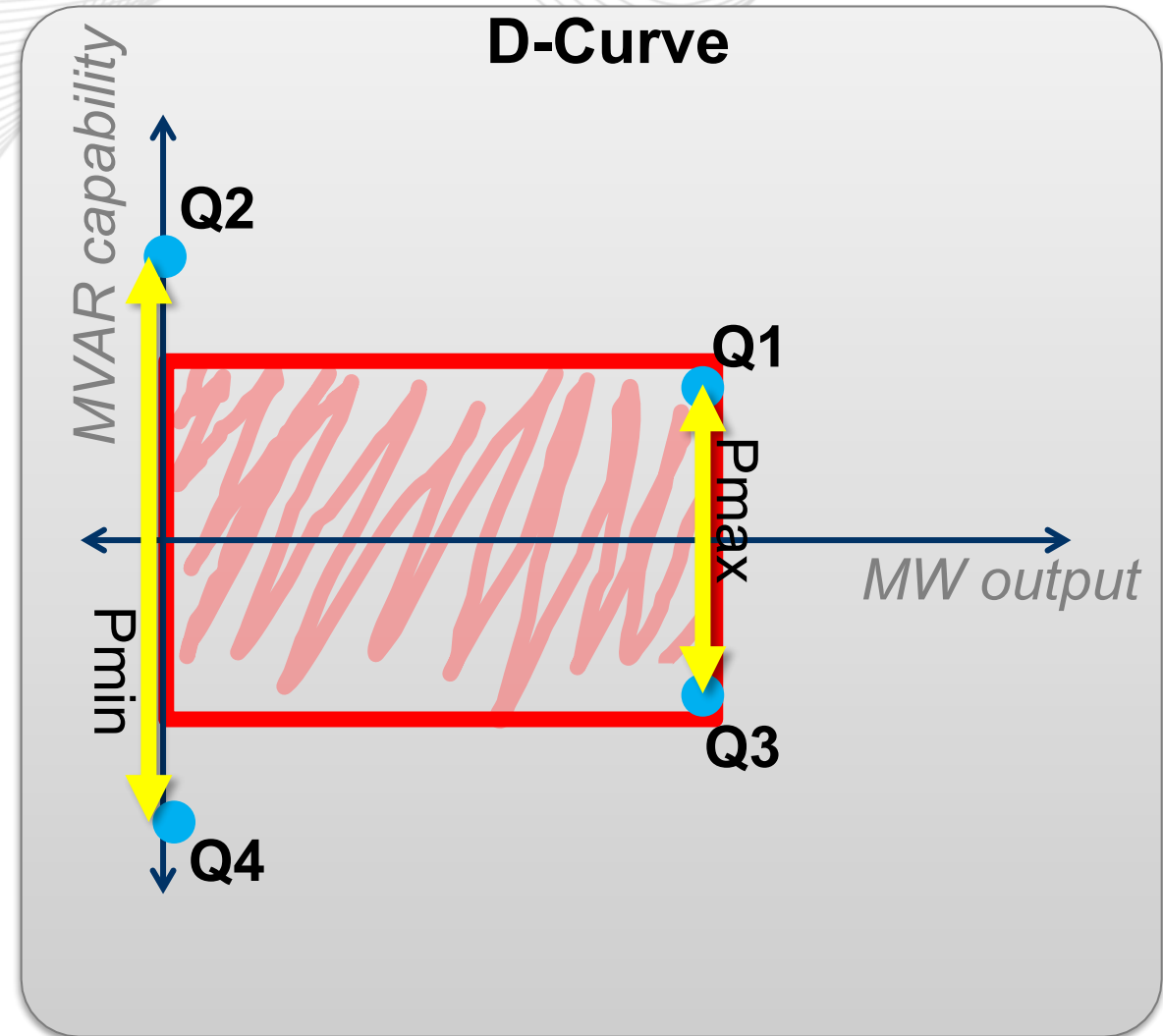


Hypothetical rate of \$1,000/MVAR-yr

Illustrative Example of Old-Technology Wind Plant w/ Full Reactive Capability at All Times

- VAR injection capability:
 - Q1 = **33** MVAR
 - Q2 = **33** MVAR
- VAR withdrawal capability:
 - Q3 = **-33** MVAR
 - Q4 = **-33** MVAR
- Average(**33,33**) – Average (**-33,-33**) = 66
- Compensation = \$1,000*66 = **\$66,000/yr**

Old wind generator technology is only partly inverter based. They don't use the generators for reactive, instead using dedicated equipment that doesn't vary with power output..



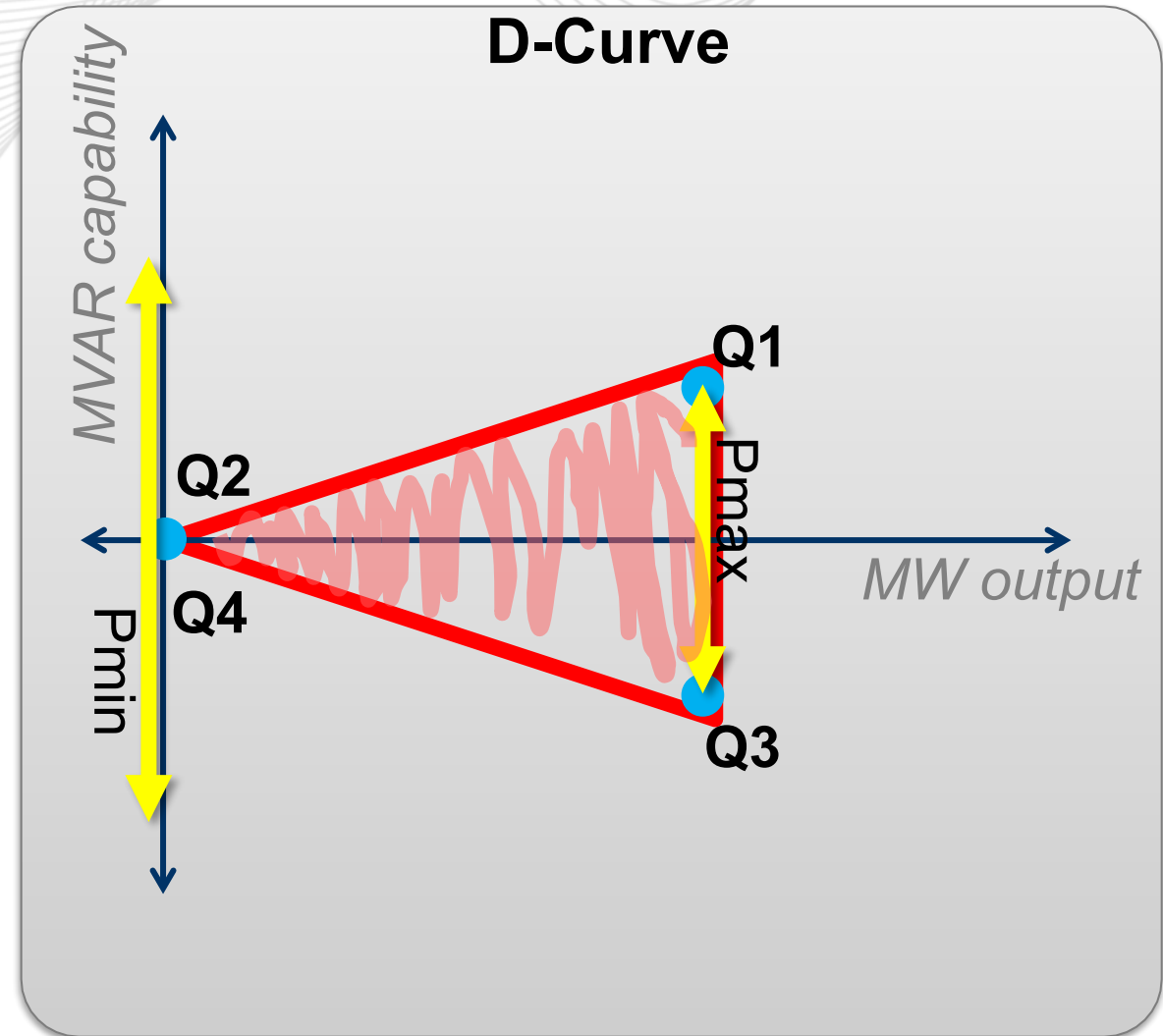
Hypothetical rate of \$1,000/MVAR-yr



Illustrative Example of Old-Technology Wind Plant w/ Fixed Power Factor Control Only as-per ISA

- VAR injection capability:
 - Q1 = **33** MVAR
 - Q2 = **0** MVAR
- VAR withdrawal capability:
 - Q3 = **-33** MVAR
 - Q4 = **-0** MVAR
- Average(**33,0**) – Average (**-33,-0**) = 33
- Compensation = \$1,000*33 = **\$33,000/yr**

This example's dedicated VAR equipment was programmed to only provide reactive capability required by the ISA, which is a fixed power factor that drops with lower MW. This is consistent with the ISA power factor obligation, but does not provide the full capability of the equipment.



Hypothetical rate of \$1,000/MVAR-yr